

LTCC Course Syllabus

Title: Combinatorial Optimisation: Packing, Partitioning, and Covering (Advanced)

Basic Details:

- Core Audience: All Ph.D. students in Pure and Applied Mathematics
- Course Format: 5x2hr lectures held in person
- Time: Every Monday, 13:00-15:00 from Jan 9, 2023 till Feb 6, 2023
- Location: Burnside Room, De Morgan House, Russell Square, London

Lecturer Details:

- Lecturer: Ahmad Abdi
- Home institution: London School of Economics and Political Science
- Location: Room 5.07, Columbia House, Houghton St, London
- E-mail address: a.abdi1@lse.ac.uk
- Telephone number: 020 7955 7325

Course Description:

Packing, partitioning, and covering are basic problems that lie at the heart of almost every problem in Combinatorial Optimisation. In this course, we study important examples of such problems in Graph Theory, namely, vertex colouring, maximum matching, and multicommodity flows. This leads us to the theories of perfect and weakly bipartite graphs. We also cover the structural, polyhedral, and algorithmic aspects of such graphs.

Prerequisites: Basic knowledge of graph theory, linear programming, and algorithms

Format:

- Five sets of electronic lecture notes.
- Five sheets of exercises appended to the end of each set of lecture notes.

Outline:

Lecture 1: Minimum vertex colouring, Tutte-Berge formula for maximum matchings, Edmonds' Blossom Algorithm, postman sets in graphs

Lecture 2: Chromatic number, maximum cliques, perfect graphs, Meyniel graphs

Lecture 3: Multicommodity flows, the cut condition, weakly bipartite graphs

Lecture 4: Blocking and anti-blocking polyhedra, perfect matrices, ideal matrices

Lecture 5: Separation vs. optimisation in linear programming, semidefinite programming, algorithms for perfect and weakly bipartite graphs

Recommended reading: The course will be self-contained. Lecture notes shall be posted after each lecture. For extra reading, please see below.

1. G. Cornuéjols: Combinatorial Optimization: Packing and Covering. SIAM (2001)
2. W. Cook, W. Cunningham, W. Pulleyblank, A. Schrijver: Combinatorial Optimization. Wiley (1997)
3. A. Abdi: Lecture notes in Packing and Covering. Available [here](#) (2018)